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Strengthening mechanisms of graphene sheets in aluminium matrix nanocomposites

A. Fadavi Boostani\textsuperscript{a}, S. Yazdani\textsuperscript{b}, R. Taherzadeh Mousavian\textsuperscript{b}, S. Tahamtan\textsuperscript{c}, R. Azari Khosroshahi\textsuperscript{b}, D. Wei\textsuperscript{d}, D. Brabazon\textsuperscript{e}, J.Z. Xu\textsuperscript{c}, X.M. Zhang\textsuperscript{c}, Z.Y. Jiang\textsuperscript{a}

\textsuperscript{a} School of Mechanical, Materials and Mechatronic Engineering, University of Wollongong, NSW 2522, Australia
\textsuperscript{b} Faculty of Materials Engineering, Sahand University of Technology, Tabriz, Iran
\textsuperscript{c} State Key Laboratory of Rolling and Automation, Northeastern University, Shenyang, Liaoning 110004, China
\textsuperscript{d} School of Electrical, Mechanical and Mechatronic Systems, University of Technology, Sydney, NSW 2007, Australia
\textsuperscript{e} Advanced Processing Technology Research Centre, School of Mechanical & Manufacturing Engineering, Dublin City University, Dublin, 9, Ireland

Abstract

Uniform dispersion of SiC nanoparticles with a high propensity to agglomerate within a thixoformed aluminium matrix was attained using a graphene encapsulating approach. The analytical model devised in this study has demonstrated the significant role of shear lag and thermally activated dislocation mechanisms in strengthening aluminium metal matrix composites due to the exceptional negative thermal expansion coefficient of graphene sheets. This, in turn, triggers the pinning capacity of nano-sized rod-like aluminium carbide, prompting strong interface bonding for SiC nanoparticles with the matrix, thereby enhancing tensile elongation.

Keywords: Metal matrix composites; Graphene sheets; Strengthening mechanisms, Fracture; Ductility

1- Introduction

Metal matrix nano-composites (MMNCs) strengthened with ceramic nanoparticles outperform the disadvantages associated with the conventional metal matrix composites (MMCs) because of the enhanced mechanical and electrical properties and the diminished coefficient of thermal expansion and friction [1]. This makes MMNCs an appropriate candidate to be employed in advanced industries such as automobile, aerospace and thermal management [1, 2].
Enhancing the tensile elongation of aluminium metal matrix composites (AMMCs) reinforced with ceramic nanoparticles, however, is a challenging task via both solid and liquid processing routes. This is attributed to the large surface-to-volume ratio and poor wettability, prompting a high degree of particulate agglomeration and imperfect interface bonding of these nanoparticles with the surrounding matrix, respectively [3, 4].

Different methods have been suggested to overcome this problem, including semi-solid stirring[5] and ball milling with ultrasonic treatment [6] but they have not been very successful. This is attributed to the fact that they have mainly concentrated on the deagglomeration of nanoparticles when they are mixing with the metallic alloy during the manufacturing process rather than in their as-received state, diminishing the efficiency of the process due to the lower wettability of these nanoparticles with most metal matrices [5, 7, 8]. Most importantly, these studies suffer from exploiting thermal models to predict the interaction of the nanoparticles with the solid/liquid interface during solidification.

Thixoforming is defined as a two-step process encompassing the preparation of a feed stock material with a thixotropic characteristic, followed by reheating the feed stock material to a semi-solid temperature in order to provide the semi-solid slurry which is then subjected to the deformation process [9-11]. This process, unlike the preceding ones, is better able to alleviate the agglomeration of the nanoparticles due to the lower mobility of these particles within the highly viscous metallic matrix during the manufacturing process, but this process by itself is still immature to effectively deagglomerate nanoparticles.

It has been reported that graphene sheets possess the unique feature of having a two-dimensional shell(s) which can nucleate and anchor nano-particles on the edges and surface [12, 13]. Authors have shown [14] that graphene nanosheets (GNSs) can confer on nanoparticles the unique capacity to resist being repelled by the advancing solid/liquid interface during solid and liquid processing.
routes. The ability of graphene sheets to alleviate the agglomeration of nano-particles during solid and liquid processing for the production of meal matrix composites, however, has hitherto not been reported.

Apart from this promising feature, to date, the actual enhancement in the thermal conductivity of SiC nanoparticles wrapped by graphene sheets and the strengthening mechanisms of graphene sheets are not well understood. This study, therefore, aims to investigate how the strengthening mechanisms of Orowan, Hall-Petch, shear lag and thermal enhanced dislocation relate to graphene reinforced AMMCs. To reach a more reliable strengthening model the thixoforming process, including forming an alloy in a semi-solid region with thixotropic behaviour, was utilized to diminish the detrimental effects of porosity associated with as-cast samples.

2- Materials and Methods

In order to prepare composite powder, i.e. preform, used for the fabrication of A357 thixoformed samples, a powder metallurgy process was utilized. This was conducted using a mixture containing SiC nanoparticles (45 nm, supplied by Nanostructured & Amorphous Materials, Inc.), graphene nanosheets (GNSs) with the average lateral size of 550 nm (supplied by Graphene Supermarket) as reinforcements and high purity aluminium powder (45 µm, supplied by Alpha Aesar Company with 99.5 % purity).

A Fritsch Pulverisette P5 planetary machine was used for ball milling without interruption under high purity (99.999%) argon gas in a liquid nitrogen environment (cryomilling) added constantly to compensate for evaporation. The stainless steel vial was sealed with an elastomeric O ring. The stainless steel balls to powder weight ratio was 15:1, and the rotation rate of the vial was 250 rpm under a total milling time of 2h. The amount of GNSs and SiC nanoparticles was adjusted to 83 Wt. % SiC and 17 Wt. % graphene. These components were milled for 0.5h without aluminium powder. Subsequently, the milling was continued for 1.5h by adding aluminium powder to the mixture
containing graphene and SiC, by setting the aluminium weight equal to 45Wt. % of the total SiC and graphene powders, in order to enhance the incorporation of the SiC nanoparticles into the molten aluminium. The prepared powder was then injected into molten A357 aluminium alloy in an atmosphere controlled with high purity (99.999%) argon gas (6 lit/min) in the semi-solid state. Table 1 demonstrates the chemical composition of the A357 alloy used in this study.

Table 1. Chemical composition of A357 alloy used in this study (Wt. %)

<table>
<thead>
<tr>
<th></th>
<th>Al</th>
<th>Si</th>
<th>Fe</th>
<th>Cu</th>
<th>Mn</th>
<th>Mg</th>
<th>Zn</th>
<th>Ti</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bal.</td>
<td>7.0</td>
<td>&lt;0.2</td>
<td>&lt;0.2</td>
<td>&lt;0.1</td>
<td>&lt;0.3</td>
<td>&lt;0.1</td>
<td>&lt;0.2</td>
<td></td>
</tr>
</tbody>
</table>

SiC nanoparticles with two different processing histories were used including (i) as received SiC nanoparticles and (ii) SiC nanoparticles encapsulated by graphene sheets (prepared, as noted above, by the milling process). After the entire alloy in the crucible was melted, it was cooled to 605 °C and held at this temperature with a solid fraction of about 0.30 [15]. The stirring process was conducted on the semi-solid alloy (using a graphite impeller) at 400 rpm associated with uniform adding of prepared powders over a time period of approximately 5 min associated with adding 1Wt. % Mg as a wetting agent. A non-contact ultrasonic process was then implemented during casting using an ultrasonic chamber (Bandelin-Germany Make – Model: RK – 100H), which can vibrate at a frequency of 35 kHz. After the completion of particle feeding, mixing was continued for an extra 1 minute. Finally, the composite slurry was poured into a pre-heated cast iron mould using a bottom-pouring system to prepare the semi-solid billet. The thixoforming process was conducted on the prepared billets based on the procedure described by S. Kandemir at a fabrication temperature of 580 °C, i.e. $T_{\text{Fabrication}}$, with continuous application of thixoforming pressure to room temperature, i.e. $T_{\text{test}}=25$ °C [16]. Table 2 represents a nomination system used to identify different specimens in the rest of this paper.
Table 2: Nomination system of the specimens

<table>
<thead>
<tr>
<th>Name used in the paper</th>
<th>Different treatment applied on samples</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Thixoforming</td>
</tr>
<tr>
<td>A357</td>
<td>-</td>
</tr>
<tr>
<td>Thix</td>
<td>*</td>
</tr>
<tr>
<td>GThix</td>
<td>*</td>
</tr>
</tbody>
</table>

The density of the samples was measured by the Archimedes method for at least three different samples in order to calculate the porosity of the samples. TEM analysis was performed using a Philips CM200 at an accelerating voltage of 200 kV. Fractographic investigations were conducted using field emission scanning electron microscopy (FE-SEM) performed in a JEOL JSM-7500FA. Tensile properties were measured using a Hounsfield universal test machine at a cross-head speed of 0.5 mms\(^{-1}\) for at least three samples in order to confirm the repeatability of the measurements.

3- Results and discussion

Fig. 1 demonstrates TEM images captured from the nanostructure of (a) Thix, (b) GThix and (c) the high magnification image of the GThix sample accompanied by the selected area diffraction (SAD) pattern of the rectangular area.

As shown by arrows in Fig. 1 (a), although SiC nanoparticles in the Thix sample are agglomerated at the grain boundaries, they are mostly engulfed within the grain interior in the GThix sample, as demonstrated in Fig. 1(b).

In Fig. 1(c), graphene sheets appear in the GThix sample with two different morphologies: onion like graphene shells (OLGS) and disk-shaped graphene sheets (DSGS). There is also some evidence for the formation of nano-sized rod-shaped aluminium carbide (NRAC) at the interface of the OLGS and the DSGS with the aluminium matrix, as shown by white arrows in Fig. 1(c). This has also been confirmed by the selected area diffraction (SAD) pattern of the rectangular region in Fig. 1(c) and high resolution TEM (HRTEM) picture as demonstrated in the bottom inset of Fig. 1(c).
Fig. 1: TEM micrographs of (a) Thix sample, (b) GThix samples associated with corresponding optical images as insets and (c) the high magnification image of the GThix sample accompanied by the selected area diffraction (SAD) pattern of the rectangular area.

The white arrows demonstrate the location where the reaction for the formation of NRAC is started at the damaged regions of the graphene sheets. The formation of NRAC is known to occur between the aluminium and the defective regions of the graphene sheets and can be expressed by the following chemical reaction scheme:

$$4\text{Al}(l) + 3\text{C}(s) \rightarrow \text{Al}_4\text{C}_3$$  \hspace{1cm} (1)

There is, however, no evidence for the formation of NRAC in the Thix sample and this is attributed to the lower temperature (580 °C) used for manufacturing this sample. It has been reported that
without any external source of carbon, the reaction for the formation of $\text{Al}_4\text{C}_3$ can occur between SiC reinforcements and molten aluminium using the following reaction:

$$4\text{Al}(l) + 3\text{SiC}(s) \rightarrow \text{Al}_4\text{C}_3 + 3\text{Si}$$ \hspace{1cm} (2)

The change in free energy ($\Delta G$) for this reaction is given by the following equation [17]:

$$\Delta G(\text{Jmol}^{-1}) = 113900 - 12.067\ln T + 8.92 \times 10^{-3}T^2 + 7.53 \times 10^{-4}T^{-1} + 21.5T + 3RT\ln (a_{\text{Si}})$$ \hspace{1cm} (3)

where $a_{\text{Si}}$ is the silicon chemical activity in molten aluminium, $R$ the universal gas constant and $T$ the absolute temperature (K). Eq. (3) registers a negative value for $\Delta G$ when the temperature exceeds 727 °C (1000 K) which is higher than the processing temperature of the Thix sample.

It has been asserted qualitatively that the SiC nanoparticles encapsulated by OLGS, as shown in Fig. 1(c), have a high tendency to be engulfed within the grain interior and this has been ascribed to the enhanced thermal conductivity of these particles [14].

The model presented in Eq. (4) predicts that particles with higher thermal conductivity are more prone to be engulfed within grains rather than being agglomerated at grain boundaries. The subscripts $p$ and $l$ refer to properties of the particles and the liquid, respectively.

$$K_p > K_l \text{ for engulfment}$$ \hspace{1cm} (4)

The following model (Eq. (5)) was built based on heat diffusivity [18] characteristics using thermal conductivity ($k$), specific heat ($c_p$) and density ($\rho$):

$$\frac{K_p \rho_p c_p^2}{K_l \rho_l c_l^2} > 1 \text{ for engulfment}$$ \hspace{1cm} (5)

The aforementioned model demonstrate that augmenting the thermal conductivity of particles results in increasing the possibility of their entrapment within grain boundaries due to the change of the interface shape from convex to concave [19-22].

It is also postulated that SiC nanoparticles encapsulated by graphene shells have higher thermal conductivity than the ones not wrapped by graphene shells [23, 24]. This is attributed to the fact that
the thermal conductivity of graphene shells on SiC nanoparticles is better conserved in bilayer and trilayer GNSs than in single layer GNSs [25].

The insets in Fig. 1 show the optical images of (a) Thix and (b) GThix samples, respectively. Image analysis results have shown a considerable reduction in the grain size of the GThix samples (D=14μm) compared with the Thix samples (D=30μm), substantiating the refining effect of well-dispersed SiC nanoparticles in the GThix sample rather than thixoforming pressure in the Thix sample. Fig. 2 shows the stress-strain curves of samples studied associated with schematic pictures representing their real microstructure. As can be seen from Fig. 2, the graphene encapsulating process has enhanced significantly the tensile properties of the PGT samples.

![Stress-strain curve](image)

**Fig.2.** Stress-strain curve of A357, Thix and GThix samples accompanied with schematic illustration of their nanostructures.

Table 3 represents the tensile properties and porosity content of the samples resulting from the analysis of different samples. According to Table 3, the yield strength (σ_{YS}) and ultimate tensile strength (σ_{UTS}) of the GThix sample are considerably higher than the Thix sample by 81% and 60%, respectively, and this is ascribed to the uniform distribution of SiC nanoparticles and the lower porosity of this sample.
Table 3: The average values of yield stress ($\sigma_{YS}$), ultimate tensile strength ($\sigma_{UTS}$), total elongation (E %) and porosity content of samples

<table>
<thead>
<tr>
<th>Samples</th>
<th>$\sigma_{YS}$</th>
<th>$\sigma_{UTS}$</th>
<th>Elongation (E %)</th>
<th>Porosity (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>A357</td>
<td>75±2</td>
<td>125±3</td>
<td>2±0.3</td>
<td>3±0.1</td>
</tr>
<tr>
<td>Thix</td>
<td>221±7</td>
<td>326±10</td>
<td>5.4±0.3</td>
<td>0.9±0.2</td>
</tr>
<tr>
<td>GThix</td>
<td>401±11</td>
<td>523±13</td>
<td>12.1±0.5</td>
<td>0.5±0.2</td>
</tr>
</tbody>
</table>

$\pm$: Represents 95 pct. confidence interval.

Fig. 3(a) represents the cleavage fracture surface of the Thix sample which is attributed to the agglomeration of SiC nanoparticles in this sample, as shown by arrows.

![Fig. 3(a) - Cleavage fracture surface of Thix sample](image1)

![Fig. 3(b) - Well-dispersed SiC nanoparticles](image2)

This agglomeration increases the probability of particle cracking associated with a higher crack propagation rate due to the settlement of these particle at the grain boundaries, thereby diminishing the ductility.

Fig. 3(b), in contrast, shows that well-dispersed SiC nanoparticles in the GThix sample are not prone to cracking or interfacial decohesion. The former is attributed to the lower possibility of cracking associated with nanoparticles and the latter can be attributed to the higher levels of plastic constraint exerted by the NRAC formed at the interface of OLGS and DSGS with aluminium, as shown by arrows in Fig. 1(c) and in the bottom inset of Fig. 3(b), respectively. The aforementioned plastic constraint is fortified by the expansion of OLGS and DSGS during solidification due to the
exceptional negative thermal expansion coefficient of graphene, thereby effectively prompting the mechanical bonding, i.e. pinning, of the SiC nanoparticles to the matrix.

These, in turn, trigger matrix cavitation through the aluminium matrix, postponed to higher strain fields, i.e. prolonged ductility. To have a better insight into the degree of strain imposed on the NRAC nucleated at the interface of SiC nanoparticles encapsulate by graphene sheets and an aluminium matrix, Eq. (6) was developed by J. F. Nye [26] to calculate the strain value exerted on the interface due to the mismatch between the thermal coefficient expansion between the graphene and surrounding aluminium matrix:

\[ \varepsilon^T = \int_{T_R}^{T_F} (\alpha_M - \alpha_G) \, dT \approx \Delta \alpha \Delta T \]  

(6)

Where \( T_F \), \( T_R \), \( \Delta T \), \( \alpha_M \) and \( \alpha_G \) represent the fabrication temperature (580°C), room temperature (25°C), difference between the fabrication temperature and room temperature, thermal expansion coefficient of matrix and graphene sheets, respectively. Table 4 lists the pertinent physical and mechanical properties of the composite constituents.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Unit</th>
<th>Al</th>
<th>SiC</th>
<th>Graphene</th>
</tr>
</thead>
<tbody>
<tr>
<td>Burgers vector (b)</td>
<td>nm</td>
<td>0.25</td>
<td>—</td>
<td>Not fixed</td>
</tr>
<tr>
<td>Thermal expansion coefficient (( \alpha ))</td>
<td>( \times 10^{-6} /^\circ C )</td>
<td>21.4</td>
<td>4.3</td>
<td>-6</td>
</tr>
<tr>
<td>Shear modulus (G)</td>
<td>MPa</td>
<td>25</td>
<td>—</td>
<td>250</td>
</tr>
<tr>
<td>Young modulus (GPa)</td>
<td>GPa</td>
<td>70</td>
<td>427</td>
<td>1000</td>
</tr>
<tr>
<td>Poisson ratio</td>
<td>—</td>
<td>0.35</td>
<td>0.17</td>
<td>0.16</td>
</tr>
<tr>
<td>Taylor factor (M)</td>
<td>—</td>
<td>3</td>
<td>—</td>
<td>—</td>
</tr>
</tbody>
</table>

Having considered Eq. (6) using the values noted in Table 4, it is clear that SiC nanoparticles encapsulated by graphene sheets can impose more plastic strain on the NRAC, nucleated on the interface of graphene sheets and the aluminium matrix, compared to the SiC nanoparticles not wrapped by graphene sheets, thereby augmenting their pinning capacity.

The progressive propagation of cracks via the microvoid coalescence mechanism is also deflected and hindered by a fiber (graphene) pull-out mechanism activated by the DSGS, as shown by white
arrows in Fig. 3(b) and the top inset of Fig. 3(b). Some SiC nanoparticles in the GThix sample, however, are agglomerated with a high tendency to cracking, as shown by the white circle in Fig. 3(b), promoting cracking that can be blocked by the graphene pull-out mechanism.

This study aims at presenting a new analytical model (Eq. (7)) by incorporating a modified shear-lag model (continuum mechanics approach) and an enhanced dislocation density model (micromechanics strengthening approach) into the model proposed by Ramakrishnan [31], as the latter generally is used for micron-sized particles.

\[
\sigma_y^{GThix} = \sigma_y^{Thix}(1 + \omega_L^{DSGS})(1 + \omega_T)(1 + \omega_{O\text{rowan}}^{DSGS} + \omega_{O\text{rowan}}^{OLGS}) + \sigma_y^{Hall-Petch}\left(\sigma_i + \frac{k}{\sqrt{D}}\right) \tag{7}
\]

Equation (7) takes into account the strengthening effects of graphene sheets, manifested in the form of load bearing \((\omega_l)\), thermal enhanced dislocation density \((\omega_T)\), and the Orowan \((\omega_{O\text{rowan}})\), and Hall-Petch mechanisms, on the yield strength of the Thix sample \((\sigma_y^{Thix})\) in order to approximate the yield strength of the GThix sample \((\sigma_y^{GThix})\).

Regarding Hall-Petch strengthening, the \(\sigma_i\), k and D define the intrinsic stress of the material \((\sigma_i = 15.7 \text{ MPa})\) and k is the material constant \((k = 0.068 \text{ MPa/M}^{0.5})\) for aluminium[32]. The Hall-Petch relationship has shown a 33.87 MPa enhancement in the yield strength of the GThix sample due to the refining effect of SiC nanoparticles encapsulated by graphene sheets. To have a subtle approximation of \(\sigma_y^{GThix}\), it is crucial to determine strengthening contributors including \(\omega_l\), \(\omega_T\), \(\omega_{O\text{rowan}}^{DSGS}\) and \(\omega_{O\text{rowan}}^{OLGS}\) in Eq. (7).

It is generally agreed that the load transfer from the ductile matrix to the hard reinforcements (i.e. ceramic and graphene) under an applied external load contributes to the strengthening of the base material according to the modified shear lag model proposed by Nardone and Prewo [33]. To investigate the concept of load transfer from the composite matrix to the embedded DSGS and OLGS, the classical shear lag model [34] was used. For this reason the two-dimensional elastic
configuration was considered for a platelet of length L, thickness t and elastic modulus E, bonded to a matrix material of thickness \( \lambda \).

The stress–strain relation along the axial direction of the platelet is \( \sigma_f = E \varepsilon_f \), where \( \sigma_f \) denotes the axial stress and \( \varepsilon_f \) the axial strain in the platelet. The equilibrium of the forces along the length of the platelet is achieved using Eqs. (8) and (9).

\[
\tau_p dx = -td\sigma_f \tag{8}
\]

\[
\frac{\tau_p}{t} = -\frac{d\sigma_f}{dx} \tag{9}
\]

It is supposed that the matrix surrounding the graphene platelet can be displaced (\( \delta \)) in the \( z \) direction and the shear strain (\( \gamma \)) is calculated using following Eq. (10).

\[
\gamma = \frac{d\delta}{dz} \tag{10}
\]

Having considered the shear stress modulus of the matrix, Eq. (10) can be rewritten in the form of Eq. (11) under the assumption that the shear stress of the matrix is transferred to the graphene platelet (\( \tau = \tau_p \)) via the graphene/matrix interface, as long as this interfacial bonding is perfect, which seems reasonable because of the negative thermal expansion coefficient of the graphene, as shown in Table 2.

\[
\frac{d\delta}{dz} = \frac{\tau_p}{G_m} \tag{11}
\]

Where \( G_m \) represents the shear modulus of the matrix, i.e. aluminium. The integration of Eq. (11) using the boundary conditions of \((z = \frac{t}{2} \text{ at } \delta = \delta_f)\) and \((z = \frac{\lambda}{2} \text{ at } \delta = \delta_\lambda)\) results in Eq. (12).

\[
\delta_\lambda - \delta_f = \left(\frac{\tau_p}{2G_m}\right)(\lambda - t) \tag{12}
\]

To approximate the strain of the graphene platelet and the surrounding matrix, displacements in Eq. (12) can be converted to strain by considering that \( e_f = \frac{d\delta_f}{dx} \) and \( e_m = \frac{d\delta_m}{dx} \). So, differentiating Eq. (12) with respect to \( x \), using Eq. (9) and the noted strains (\( e_f \) and \( e_m \)), results in Eq. (13):
By considering that generally $\lambda \gg t$ and multiplying Eq. (13) by $E_f$, Eq. (13) can be written in the form of Eq. (14):

$$\frac{d^2\sigma_f}{dx^2} = \left(\frac{n^2}{t^2}\right)(\sigma_f - e_m E_f) \tag{14}$$

In this equation, $n$ can be defined as $n = \sqrt{\frac{2\mu_m}{E_f} \left(\frac{L}{\lambda}\right)}$. Then the general solution for this differential equation can be written as:

$$\sigma_f = E_f e_m + C \sinh\left(\frac{nx}{t}\right) + D \cosh\left(\frac{nx}{t}\right) \tag{15}$$

Using the boundary conditions that if $x = 0$, then $\sigma_f = E_f e_m$ and if $x = \frac{L}{2}$, then $\sigma_f = 0$, the constants $C$ and $D$ for Eq. (15) are achieved. Hence, the final solution of Eq. (15) can give the stress distribution along the length of the graphene platelet as Eq. (16):

$$\sigma_f = E_f e_m \left[1 - \frac{\cosh\left(\frac{nx}{t}\right)}{\cosh\left(\frac{nt}{2}\right)}\right] \tag{16}$$

Additionally using Eq. (16) the interfacial shear stress for the graphene platelet can be calculated according to Eq. (17):

$$\tau_P = n E_f e_m \left[\frac{\sinh\left(\frac{nx}{t}\right)}{\cosh\left(\frac{nt}{2}\right)}\right] \tag{17}$$

Having considered the aspect ratio of the graphene plate and the matrix strain $(\epsilon_m)$, let $(s = \frac{L}{t})$, Eq. (16) and (17) can be rewritten in the following forms [35]:

$$\sigma_f = E_f e_m \left[1 - \frac{\cosh\left(ns\frac{x}{t}\right)}{\cosh\left(\frac{nt}{2}\right)}\right] \tag{18}$$

$$\tau_P = n E_f e_m \left[\frac{\sinh\left(s\frac{x}{t}\right)}{\cosh\left(\frac{nt}{2}\right)}\right] \tag{19}$$
Therefore, the maximum load transfer from the matrix to the graphene platelet is attainable for the composite with the higher value of \( n_s \). To reach this, it is necessary to reduce the distance between the graphene platelets (\( \lambda \)) and simultaneously diminish their thickness, as thickness (\( t \)) affects the \( n \) with square root but it has an inverse relationship with \( S (S=L/t) \). At this stage, it is also necessary to introduce a new parameter to correlate the \( n_s \) value of the graphene platelet with the load-bearing improvement factor (\( \omega_l \)) affected mainly by the volume fraction of the reinforcements [31]. To find the \( \omega_l \) value, it is imperative to ascertain the inter-particle spacing, as a function of the total graphene volume fraction (\( V_{Gr} \)). Hence, the \( \omega_l \) parameter is defined as:

\[
\omega_l = \sqrt{\frac{2G_mL^2}{E_f \lambda_{eff} t}}
\]  
(20)

Where \( \lambda_{eff} \) is an effective inter-particle spacing between the graphene sheets within the matrix, and can be calculated using Eqs. (21) and (22) [36]:

\[
\lambda_{eff}^{DSGS} = 0.931 \sqrt{\frac{0.306\pi dt}{V_{Gr}^{DSGS}}} - \frac{\pi d}{8} - 1.061t
\]  
(21)

Where \( d, t \) and \( V_{Gr}^{DSGS} \) is the length, thickness and volume fraction of DSGS, respectively, and is measured by image analysis of at least 20 HRTEM micrographs.

Putting the values of \( t=10 \) nm, \( \lambda_{eff}=427 \) nm (calculated by Eq. (21)) and the values provided in Table 2 into Eq. (20) results in \( \omega_l=0.15 \) for DSGS.

It should be noted that the \( V_{Gr}^{DSGS} \) and \( V_{Gr}^{OLGS} \) have been set to 0.18\% and 0.82\% of the total volume of the graphene (\( V_{Gr}=0.01 \)) added as a raw material, respectively, and is measured along with other microstructural features such as \( L \) and \( t \) using image analysis of at least 20 HRTEM micrographs.

The aforementioned calculations represent the significant effect of OLGS on load transfer and the subsequent strengthening the aluminium matrix compared to DSGS due to the lower thickness and angled formation of the NRAC in the former, fortifying the pinning and thereby the load transfer from the matrix to the SiC nanoparticles.
According to Table 2, exceptional difference in the thermal expansion coefficient of graphene compared to aluminium can significantly strengthen the aluminium matrix by generating thermally induced dislocation, as shown in Fig. 1(c), reaffirmed by a high strengthening contributor \( \omega_T \) calculated by Eq. (22) [37].

\[
\omega_T = \frac{1.25 \sigma_m b}{G_m \mu_{Thix}} \sqrt{\frac{12 \left( T_{Fabrication} - T_{test} \right) \left( \alpha_m - \alpha_{Gr} \right) V_{Gr}}{b d_{Gr} (1 - V_{Gr})}}
\]

Eq. (22) can be solved based on the values presented in Table 2, \( V_{Gr} \) is the total volume fraction of the graphene encompassing the graphene sheets and the shells encapsulating the SiC nanoparticles (0.01), \( d_{Gr} \) is related to the average diameter of the graphene sheets and shells within the aluminium matrix (45 nm), and \( \sigma_y^{Thix} \) is the yield strength of the Thix sample (221 MPa), resulting in \( \omega_T = 0.14 \).

To determine the strengthening contribution of DSGS and the OLGS under the Orowan strengthening mechanism, two different models can be utilised [36].

\[
\omega_{Orowan}^{DSGS} = \frac{M G b}{2 \pi \sqrt{1 - \sigma_y^{Thix}}} \left( \frac{1}{0.931 \left( \frac{0.706 A d_t}{V_{Gr}^{Disc}} \frac{\pi d}{8} - 1.061 t \right)} \right) \ln \frac{1.225 t}{b}
\]

\[
\omega_{Orowan}^{OLGS} = \frac{M G b}{2 \pi \sqrt{1 - \sigma_y^{Thix}}} \left( \frac{0.779}{V_{Gr}^{Grion}} - 0.785 \right) \ln \frac{0.785 d}{b}
\]

The investigation of Eq. (23) and (24) using the values provided in Table 2, \( V_{Gr}^{DSGS} \) (0.0018), \( V_{Gr}^{OLGS} \) (0.0082), \( d \) (45 nm) and \( t \) (10 nm) which are the average diameter and thickness of at least 60 DSGS and OLGS measured using HRTEM analysis, respectively, gives the values of 0.13 and 0.23 for \( \omega_{Orowan}^{DSGS} \) and \( \omega_{Orowan}^{OLGS} \), respectively. It should be noted that \( V_{Gr}^{DSGS} \) (0.0018) and \( V_{Gr}^{OLGS} \) (0.0082) are the effective volume fractions of the DSGS and the OLGS calculated based on image analysis of 20 HRTEM micrographs, respectively. This shows the greater role of the OLGS as compared to the DSGS. This discrepancy is attributed mainly to the orientation in which the
DSGS interact with active slip planes during the deformation process. This can be ascribed to the fact that the DSGS are assumed to have a habit plane perpendicular to the slip plane of the aluminium (111) in Eq. (23). In practice, however, some DSGS lie on the slip plane of the aluminium matrix, resulting in lower interaction between the DSGS and dislocation gliding on the matrix slip plane.

Fig. 4 shows the strengthening contributor values corresponding to different strengthening mechanisms, as calculated in the preceding equations, demonstrating the major role of thermally activated dislocation mechanism in augmenting the yield strength compared to the other strengthening mechanisms. As shown in Fig. 4, OLGS are stronger in strengthening aluminium matrix compared to the DSGS, attributed to the circular morphologies of these graphene sheets, thereby increasing the density of dislocation more effectively compared to the DSGS.

![Fig. 4: Contribution of different strengthening mechanisms in enhancing the tensile yield strength of composite reinforced with graphene sheets.](image)

By inserting the calculated values: \( \omega_{L}^{DSGS} = 0.15 \), \( \omega_{T} = 0.42 \), \( \omega_{Orowan}^{DSGS} = 0.13 \) and \( \omega_{Orowan}^{OLGS} = 0.23 \) into Eq. (7), \( \sigma_y^{Thix} \) is envisaged to be around 490 MPa, which is close to the value obtained experimentally (401 MPa). This suggests that the devised model is worth being considered to have a
subtle approximation about the effect of incorporation of graphene sheets in enhancing the tensile properties of the metal matrix composites. The difference between the tensile properties envisaged by the models and the experimental ones is attributed to four possible reasons including (i) the total volume fraction of the DSGS is assumed to have a habit plane perpendicular to the slip plane of the aluminium (111) in the model presented, however, some of them could settle on the slip plane of the aluminium matrix resulting in lower interaction between them and resulting in gliding dislocations; (ii) graphitization through Van der Waals interactions between some graphene sheets during the manufacturing process, resulting in the formation of unwrapped-graphene and hence agglomerated SiC nanoparticles; (iii) the possibility of overwrapping SiC nanoparticles by OLGS, as the calculation relies on the existence of at least 5 OLGS and (iv) high SiC nanoparticles content stimulates the incomplete graphene encapsulation process and in turn the agglomeration of these particles, thereby levelling off the strengthening.

4- Conclusion

This study reveals the major strengthening mechanisms coming to practice by implementation of graphene sheets as reinforcement in metal matrix composites. In fact, this study demonstrates that the graphene encapsulating process not only has a unique capacity to attenuate the agglomeration of SiC nanoparticles but also has the exceptional feature in strengthening the aluminium metal matrix composites using thermally activated dislocation and pinning the SiC nanoparticles to the matrix, thereby augmenting tensile ductility significantly.

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References


Graphical Abstract
Highlights
In this paper, we have shown:

- Production of Al-SiC composite reinforced with uniform distribution of SiC nanoparticles.
- The most important strengthening mechanisms of graphene sheets in aluminium matrix nanocomposites which can be used for other metal matrix composites.
- Enhanced tensile properties especially tensile elongation of aluminum based nanocomposites.