

CLUSTERING VERTICAL GROUND REACTION FORCE CURVES PRODUCED DURING COUNTERMOVEMENT JUMPS

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Abstract

The aim of this study is to assess and compare the performance of commonly used hierarchical, partitional (k-means) and Gaussian model-based (Expectation-Maximization algorithm) clustering techniques to appropriately identify subgroup patterns within vertical ground reaction force data, using a continuous waveform analysis. In addition, we also compared the performance across each technique using normalized and non-normalization input scores. Both generated and real data (one hundred-and twenty two vertical jumps) were analyzed. The performance of each cluster technique was measured by assessing the ability to explain variances in jump height using a stepwise regression analysis. Only k-means (normalized scores; 82 %) and hierarchical clustering (normalized scores; 85 %) were able to extend the ability to describe variances in jump height beyond that achieved using the group analysis (i.e. one cluster; 78 %). Further, our findings strongly indicate the need to normalize the input data (similarity measure) when clustering. In contrast to the group analysis, the subgroup analysis was able to identify cluster specific phases of variance, which improved the ability to explain variances in jump height, due to the identification of cluster specific predic-

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tor variables. Our findings therefore highlight the benefit of performing a subgroup analysis and may explain, at least in part, the contrasting findings between previous studies that used a single group level of analysis.

Keywords: clustering, vertical ground reaction force, analysis of characterizing phases, countermovement jump

1. Introduction

The countermovement jump (CMJ) is an important task in a number of sports (e.g. volleyball, basketball) and its biomechanics have been frequently studied [16]. However, identified features that relate to the performance outcome (jump height) are often inconsistent [28]. For example, maximum vertical ground reaction force (vGRF) is reported in some studies as a performance related factor [4, 8, 30], while it is not in others [19, 21, 24]. This makes it difficult to conclude which neuromuscular capacities or movement techniques should be altered to enhance jump height, the criterion performance outcome in CMJs. Recently, we have shown that some of the contrasting findings across studies may be due to the use of discrete point analysis [28]. An alternative to discrete point analysis is a continuous waveform analysis (e.g. functional principal component analysis or analysis of characterizing phases) which has grown in popularity within many disciplines, including biomechanics, and has been reported to provide a better insight than discrete point analysis [6, 7, 9, 11, 20, 26, 28, 29].

An additional reason for the inconsistencies across studies however, may be inter-subject variability. Vertical ground reaction curves generated during

19 a CMJ can differ significantly in shape across subjects (e.g. non-modal, uni-
20 modal or bi-modal), which could imply that different movement strategies
21 are being employed, which may in turn have different performance related
22 factors. This might explain some of the contrasting findings, since previous
23 studies generally employed a single group analysis which can mask perfor-
24 mance related factors if different shapes have different performance related
25 factors [1, 32, 33]. An alternative to a single group analysis is a subgroup
26 analysis, which classifies similar patterns (curve shapes or movement strate-
27 gies) into subgroups; so called clusters. An optimal clustering maximizes the
28 ability to predict the dependent variable (e.g. jump height) of a data set [10].
29 To the authors' knowledge it appears that none of the previous CMJ studies
30 have used a subgroup analysis, while subgroup analyses have been frequently
31 performed in studies that examine human gait [2, 15, 22, 23, 34, 35, 37].

32 A challenge in subgroup analysis is that a variety of clustering techniques
33 exists that may result in different clusters [12, 13, 18, 39]. Additionally, while
34 the number of studies that have used continuous waveform analysis in the
35 area of biomechanics is increasing, little is known about the performance of
36 different clustering techniques with continuous waveform analysis in biome-
37 chanics. The computed continuous features aim to represent the pattern of a
38 curve over multiple phases of the movement cycle and can be highly collinear,
39 which may influence results of some clustering techniques. Clustering ap-
40 proaches differ in their underlying assumptions and can be divided broadly
41 into hierarchical, partitional and probabilistic clustering [12, 18, 39]. The

42 advantage of hierarchical clustering techniques is that they provide a highly
43 interpretable description of the hierarchy within the data (i.e. dendrogram)
44 and do not require the number of clusters to be chosen prior to the analysis.
45 However, the assignment of samples into clusters requires the generation of
46 inter-point distances of the input data (where different approaches can give
47 very different results) and imposes a hierarchical structure within the exam-
48 ined data [12, 18, 39]. In contrast, partitional clustering (e.g. k-means) can
49 be performed without calculating inter-point distances, it is commonly used
50 and is usually more suitable for large data sets [18]. However, k-means clus-
51 tering also requires the user to choose the number of clusters (prior to anal-
52 ysis) and the construction of a dendrogram is computationally prohibitive
53 [12, 13, 18, 39]. In addition, both hierarchical and partitional clustering
54 techniques follow a deterministic process where the generated clusters and
55 their members are somewhat dependent on the ordering of samples [39]. Con-
56 sequently, a third method, model-based clustering might be more appropriate
57 for classifying biomechanical data. Model-based clustering techniques assign
58 individuals into clusters based on their fit to a given mathematical model.
59 An often used model is the Gaussian mixture model [10], which assigns sub-
60 jects into clusters based on the nature of the statistical inference, might be
61 more appropriate for classifying movement strategies. Due to the variation
62 in clustering approaches, and the relative novelty of classifying continuous
63 biomechanical data / features, it is important to identify which clustering
64 technique has the greatest ability to recognize and appropriately separate

65 patterns within multiple curves.

66 The primary aim of this study is to assess and compare the performance
67 of commonly used hierarchical, partitional and probabilistic clustering tech-
68 niques to appropriately identify patterns within a sample of self-created
69 curves (manipulated data set) and a sample of vGRF curves captured dur-
70 ing countermovement jumps (real data set), using a continuous waveform
71 analysis. A secondary aim is to examine if there are benefits to performing
72 a subgroup analysis compared to the commonly used single group analy-
73 sis when identifying vertical ground reaction vGRF factors related to jump
74 height.

75 2. Methods

76 2.1. Data Set

77 **Manipulated Data Set** A random vGRF curve from the real data set
78 (see below) was selected and used to create a sample of 100 manipulated
79 curves, which contained three clusters to reflect some of the general shapes
80 of the vGRF curve. Curves in the first cluster ($n = 41$) were manipulated
81 to have a unimodal shape, where the peak value occurred from 25-30 % of
82 the cycle. Curves in the second cluster ($n = 9$) were manipulated to have a
83 unimodal shape, where the peak value occurred from 70-75 % of the cycle.
84 Curves in the third cluster ($n = 50$) were manipulated to have a bimodal
85 shape, where the peak value occurred from 75-80 % of the cycle (Figure 1).
86 To generate the manipulated data set the randomly selected curve was trans-

87 formed into a function, using seven coefficients and a b-spline basis system
88 [5, 25]. The third (cluster 1 and 3) and fifth (cluster 2 and 3) coefficients
89 were multiplied with a random factor between one and two, while the fourth
90 coefficient (Cluster 3) was multiplied with a random number between minus
91 one and zero. After altering the coefficients, manipulated curves were gener-
92 ated by solving the altered coefficients to 101 points. Subsequently, the peak
93 position of each curve was shifted randomly in time, using a dynamical time
94 warping approach, within a random range of -2.5 and 2.5 %. The used dis-
95 tribution was created *ipso facto* to model a realistic distribution, accounting
96 for low frequent modal shapes.

97 **Real Data Set** One-hundred-and-twenty-two male athletes (age = 22.4
98 \pm 4.2 years; mass = 71.1 \pm 9.4 kg; height = 1.82 \pm 0.1 m), who were phys-
99 ically active, experienced in performing the countermovement jump (based
100 on the sports they played: Gaelic football, hurling and basketball), and free
101 from lower limb injury participated in this study. The University Ethics
102 Committee approved the study and all participants were informed of any
103 risk and signed an informed consent form before participation.

104 Prior to data collection, every participant performed a standard warm-up
105 routine consisting of low intensity jogging, stretching and ten sub-maximal
106 and five maximal effort countermovement jumps. Each participant performed
107 15 jumps without an arm swing, standing with each foot on a separate force
108 platform. Participants rested for 30 seconds between trials. Two force plates

109 (BP-600900, AMTI, MA, USA) recorded the vGRF (1000Hz). Based on
110 jump height, the best jump performance of each subject was identified and
111 used for analysis¹. Jump height was calculated using the center of mass
112 velocity at takeoff, with take-off determined when the vGRF fell below 5 N
113 [28]. The position of the center of mass was calculated using a motion analysis
114 system (Vicon 512 M, Oxford Metrics Ltd, England) to record the position
115 of twelve reflective markers (250Hz), in combination with anthropometric
116 data [38]. Reflective markers were attached bilaterally, using double sided
117 tape, on the following anatomical landmarks: fifth metatarsal joint, posterior
118 calcaneus (in line with the fifth metatarsal joint), lateral malleolus, lateral
119 femoral epicondyle, greater trochanter and the glenohumeral joint. All curves
120 were normalized to body mass and only the vGRF-time curve during the
121 propulsion phase was analyzed because it holds the information needed to
122 fully describe jump height. The start of the propulsion phase was identified
123 from the power-time curve of the body's centre of mass, when the power
124 became positive.

125 *2.2. Data Clustering*

126 To generate scores that capture the patterns within the continuous wave-
127 forms, an Analysis of Characterizing Phases was performed [28]. Analysis
128 of Characterizing Phases detects phases of variation (key phases) within the

¹The best jump was used because it is a well-defined criterion and avoids taking an average of multiple curves which may have distorted the data.

129 sample of curves, which are used to generate participants' scores (similarity
 130 score). Similarity scores were computed for key phases using the magnitude
 131 domain. The number of similarity scores extracted for each waveform is equal
 132 to the number of identified key phases. Similarity scores were determined by
 133 calculating the area between a participant's curve (p) and the mean curve
 134 across the data set (q) for every point (i) within the key phases (Equation 1)².

$$\textit{similarity score} = \int p_i - q_i \quad (1)$$

135 Key phases were identified using the information generated by the prin-
 136 cipal components needed to describe 99.5 % of the variances in the data [27].
 137 To increase the interpretability of the retained principal components a VARI-
 138 MAX rotation was performed [11, 26]. For further explanation of Analysis
 139 of Characterizing Phases the reader is referred to a previous paper by the
 140 authors [28]. Given that Analysis of Characterizing Phases generates just
 141 a few similarity scores to describe a complex waveform, it was necessary to
 142 insure that the generated scores preserve the information needed to cluster
 143 curves with similar patterns (shapes). The quality of the preserved infor-
 144 mation was estimated, for only the manipulated data set, by a subjective
 145 visual inspection of the generated similarity scores and was judged sufficient

²The used equation can result in a similarity score close or equal to zero when a subject and the reference signal are opposite or when a signal oscillates above and below the references signal. In the present study, the shape of the reference and subject curve followed a similar pattern within the key phases.

146 since a clear linear relationship exists for curves within each cluster (Figure
147 2). The reader should note that the calculation of subject score within the
148 present paper differs slightly from Richter et al. [28] to overcome a depen-
149 dency of the finding on the reference signal chosen. In Richter et al. [28]
150 the best jump was selected as reference signal because the subject score cal-
151 culation used absolute values to measure similarity. This approach assumes
152 that altering a curve towards the reference signal has a positive effect on
153 the dependent variable. However, this might not be true as other movement
154 strategies might represent a better movement solution. The score generation
155 approach used in the present paper overcomes this limitation and findings
156 are not dependent on the reference signal. The overall mean was selected as
157 the reference signal because it is commonly used and easy to relate to when
158 interpreting the findings.

159 To classify the manipulated and real data sets the computed similar-
160 ity scores were input into a hierarchical clustering algorithm (hierarchical
161 clustering), a k-means approach (partitional clustering) and an Expectation-
162 Maximization algorithm (model-based clustering). Due to the linear relation-
163 ship between similarity scores within a cluster, where clusters could overlap
164 in space possibly hampering the ability of the hierarchical and the k-means
165 clustering, the hierarchical and the k-means clustering were also performed
166 using normalized similarity scores (as suggested in Jain et al. [13]). The
167 normalization was performed by transforming the similarity scores into their
168 correlation matrix (Equation 2), to quantify numerically the relationship be-

169 tween the similarity scores, which cannot be described by distances of the
 170 generated similarity scores. The correlation matrix (\hat{P} ; $\hat{P} \in \mathbb{R}^{122 \times 122}$) was cre-
 171 ated by calculating the Pearson's r-value (*corr*) utilizing the similarity scores
 172 (*SS*) of the curves i ($i = 1, 2, \dots$, number of curves) and j ($j = 1, 2, \dots$,
 173 number of curves).

$$[\hat{P}]_{(i,j)} = corr_{(i,j)} = \frac{1}{N-1} \sum_{k=1}^N \frac{(SS_{i,k} - \mu_i) * (SS_{j,k} - \mu_j)}{\sigma_i * \sigma_j} \quad (2)$$

174 where μ is the average and σ the standard deviation for curve i and
 175 j of their corresponding similarity scores, which were calculated using the
 176 identified key phases ($k = 1, 2, \dots, N$, where N is the number of identified
 177 key phases).

178 The hierarchical algorithm calculated pairwise distances using Euclidean
 179 distance, and created a hierarchical cluster tree using the nearest distance
 180 [18]. The quality of the hierarchical clustering was measured by calculating
 181 the cophenetic correlation coefficient between the hierarchical cluster tree
 182 and the pairwise distances [18, 31]. Hierarchical clustering properties were
 183 changed if the cophenetic correlation coefficient was less than 0.7, which
 184 indicates a low or medium correlation between the hierarchical cluster tree
 185 and the pairwise distances³ [3]. The k-means clustering technique used the
 186 squared Euclidean distance as the distance measure and the Expectation-

³All generated hierarchical cluster trees and the pairwise distances generated a cophenetic correlation coefficient above 0.7

187 Maximization algorithm was applied using the Gaussian mixture model [18].

188 For the manipulated data, the performance of each clustering technique
189 was assessed by the percentage of accurately classified curves, assessed by
190 counting how often the assigned membership and the actual membership of
191 a curve matched. To examine the benefits of using a subgroup analysis, key
192 phases were identified using both a single group and a subgroup analysis,
193 and directly compared. The number of clusters in the subgroup analysis was
194 set at three clusters due to the contained number of general shapes (three
195 shapes).

196 For the real data set, the performance of each clustering technique was
197 measured by assessing the ability to explain variances in jump height (de-
198 pendent variable) across generated clusters. This approach was based on the
199 assumption that an appropriate grouping of vGRF curve shapes (or similar
200 movement strategies) does not mask performance related factors and hence
201 enhances the ability to describe variances in jump height. To assess the abil-
202 ity to explain variances in jump height for a given number of clusters the
203 average r^2 -value of a stepwise regression analysis was computed across these
204 clusters. The clustering technique with x clusters that generated the highest
205 ability to explain variances in jump height was considered the most appro-
206 priate clustering technique for the captured vGRF curves. Input variables
207 for the regression model were similarity scores measured solely over the key
208 phases of a cluster. During the clustering process two problems can occur for
209 a given cluster solution: (a) the regression analysis does not identify a predic-

210 tor variable and, (b) only one subject is assigned to a cluster. If the stepwise
211 regression analysis was not able to identify any predictor variables, the high-
212 est r^2 -value computed during the correlation analysis between the generated
213 similarity scores and jump height was used (irrespective of whether it was
214 statistically significant or not)⁴. If a given cluster solution assigned only one
215 participant to a cluster, the cluster and its member were considered as an
216 outlier and removed from the analysis.

217 If the stepwise regression analysis was not able to identify any predictor
218 variables within a cluster, the highest r^2 -value (irrespective of its significance)
219 computed during the correlation analysis (between the generated similarity
220 scores and jump height) was used. If a cluster technique assigned only one
221 participant to a cluster, the cluster was discarded.

222 To examine the benefits of a subgroup analysis over a single group analysis
223 both the key phases and the predictor variables were compared when calcu-
224 lated for the whole data set (single group) to the key phases the predictor
225 variables selected within each of the generated clusters (subgroup analysis).
226 The number of clusters was set to increase from one to ten clusters. All
227 statistical analyses were performed using MatLab (R2012a, MathWorks Inc.,
228 USA).

⁴It should be noted that for the cases where no predictor variable was identified by the regression analysis, the sample size of the corresponding cluster was low and the correlation of an independent variable to the dependent variable was not high enough to reach a significant correlation.

229 **3. Results**

230 *3.1. Manipulated Data Set*

231 For the manipulated data set, the accuracy of the clustering techniques
232 was (from high to low): hierarchical clustering utilizing normalized scores
233 (98 % accuracy), k-means clustering utilizing normalized scores (97 % ac-
234 curacy), Expectation-Maximization algorithm (95 % accuracy), hierarchical
235 clustering utilizing similarity scores (67 % accuracy) and k-means clustering
236 utilizing similarity scores (61 % accuracy).

237 Key phases differ between the single group and subgroup analysis. Key
238 phases for the whole group analysis were identified at 20-30 %, 45-57 % and
239 72-82 % of the movement cycle. The key phases for each cluster, examined
240 using a subgroup analysis were identified at 22-36 % and 82-91 % for cluster
241 1, 55-67 % and 78-87 % for cluster 2, and 60-68 %, and 81-89 % of the
242 movement cycle for cluster 3.

243 *3.2. Real Data Set*

244 For the real data set, predictor variables (similarity scores computed from
245 key phases), identified by the stepwise regression analysis, were able to ex-
246 plain 78 % of the variances in jump height ($r^2 = 0.78$). Hierarchical clus-
247 tering (normalized scores) best described jump height using four clusters (85
248 %) and k-means (normalized scores) performed best using four clusters (83
249 %). The Expectation-Maximization algorithm, hierarchical clustering (sim-
250 ilarity scores) and the k-means (similarity scores) were not able to increase

251 the ability to describe jump height over that achieved using the single group
252 analysis (Figure 3).

253 Hierarchical (normalized scores) clustering explained most accurately the
254 variances in jump height but generated two clusters with sample sizes less
255 than ten members (Cluster 1 = 7; Cluster 3 = 6). For the clusters with
256 small sample sizes, the regression analysis was not able to identify predictor
257 variables. Hence, k-means (normalized scores) clustering was selected for
258 further analysis, as it had almost the same ability to describe variance in
259 jump height with larger sample sizes and better-balanced cluster sizes. Visual
260 inspection of the mean curves of the generated k-means (normalized scores)
261 clusters indicates four distinct vGRF curve shapes: (cluster 1) unimodal with
262 high initial vGRFs where peak vGRF occurs shortly after the start of the
263 concentric phase, (cluster 2) unimodal with low initial vGRF where peak
264 vGRF occurs at about 70 % of the movement cycle, (cluster 3) bimodal with
265 high initial vGRFs where peak vGRF occurs shortly after the start of the
266 concentric phase, and (cluster 4) bimodal with initial vGRFs similar to both
267 the first and second maxima where peak vGRF could occur either before 15
268 % or around 80 % of the movement cycle (Table 1; Figure 4). No significant
269 difference exists in jump height across the clusters.

270 Key phases and identified predictor variables differed between the single
271 group and subgroup analysis, while the strongest relation to jump height
272 occurred at around 85 % across both subgroup and single group analysis
273 (Figure 5). All predictor variables were identified by the stepwise regression

274 analysis. The reader should note that the subgroup analysis was able to
275 increase the ability to describe jump height, while using fewer data points (a
276 smaller percentage) of the movement cycle.

277 **4. Discussion**

278 *4.1. Clustering Technique Comparison*

279 The examined clustering techniques differed in their performance in both
280 the manipulated and real data sets. Using the manipulated data, the hi-
281 erarchical clustering utilizing normalized scores, k-means clustering utilizing
282 normalized scores, and Expectation-Maximization algorithm performed best.
283 Using the real data set, only k-means (normalized scores) and hierarchical
284 clustering (normalized scores) extended the ability to describe variances in
285 jump height beyond that achieved using the group analysis (e.g. one clus-
286 ter). With respect to the Expectation-Maximization algorithm, it was not
287 able to generate clusters with a higher ability to describe variances in jump
288 height than that achieved at a single group level (i.e. one cluster). While the
289 Expectation-Maximization algorithm was successful for the generated data
290 set, it failed to successfully classify the real data. A possible reason for this
291 contrasting performance lies in the nature of both data sets. The manipu-
292 lated data set holds clear distribution patterns where peak vGRF differed
293 across curves within a cluster by only ± 5 %. The real data set, however,
294 has much more variation and the probability distribution does not differ as
295 clearly across clusters (Figure 6).

296 *4.1.1. Benefits of Normalizing Data*

297 Normalizing similarity scores (transformation of scores into their corre-
298 lation matrix) had a significantly positive effect on the performance of both
299 hierarchical and partitional clustering techniques, indicating that differences
300 in magnitude between similarity scores are not as effective as their quanti-
301 fied numerical relationship at maximizing the ability to predict a dependent
302 variable. The same effect is likely to occur when discrete points are used
303 for clustering individuals. To the best of our knowledge, previous studies
304 that aimed to identify movement patterns by clustering discrete kinematic
305 and kinetic variables did not normalize their input variables, which may
306 have reduced their ability to recognize movement patterns [2, 15, 17, 22, 34].
307 To date, no study has compared clustering approaches using biomechanical
308 waveforms, which makes it difficult to control the effect of normalizing the
309 input data. For this reason we applied k-means clustering to a publicly avail-
310 able data set (The Berkeley Growth Data: Tuddenham and Snyder [36]). The
311 Berkeley Growth Data has been used to measure the accuracy of k-means
312 clustering (e.g. Jaques and Preda [14]) and, similar to vGRF curves, the
313 shapes of the sample of curves might hold the information needed to classify
314 the data correctly. Applying k-means to the Berkeley Growth Data using
315 non-normalized and normalized similarity scores resulted in clustering accu-
316 racies of 74.2 % and 94.6 %, respectively. In the experiment of Jaques and

317 Preda [14]⁵, the highest accuracy of k-means was 66.7 %. The increase in
318 accuracy of k-means in the present work is due to the effect of normalization
319 (accounting for ± 20.4 %) and the use of similarity scores (accounting for
320 ± 7.5 %). The contrasting findings between non-normalized and normalized
321 scores for hierarchical and partitional techniques (for the manipulated, real
322 and Berkeley Growth data) strongly suggest that input variables should be
323 normalized when classifying curves where the curve shape might hold im-
324 portant information. It should be noted, however, that other normalization
325 approaches (e.g. Euclidian distance) may lower the ability to recognize shape
326 pattern.

327 *4.2. Benefits of Subgroup Analysis*

328 With respect to the benefit of performing a subgroup analysis, the sub-
329 group analysis alone was able to capture key phases, which reflect specific
330 characteristics of each cluster, resulting in different locations of key phases
331 and predictor variables across clusters. These differences (Figure 5) resulted
332 in a greater ability of the subgroup analysis to describe variances in jump
333 height over a group level analysis (on average +8.3 %). In addition to this
334 increased ability to describe variances in jump height, the subgroups required
335 less information (less % of the data) to predict jump height (on average 17
336 % less of the movement cycle). While previous CMJ studies have not exam-

⁵Jaques and Preda [14], assessed the ability of k-means using non-normalized data (whole discrete curve, 20 spline coefficients and functional principal component scores)

337 ined the effectiveness of a subgroup analysis, gait studies have also shown its
338 appropriateness over a single group analysis [2, 15, 22, 34].

339 The subgroup analysis was able to identify four distinct vGRF curve
340 shapes. The characteristics of these clusters strengthen the idea that different
341 individuals may have different performance related factors [1, 32, 33]. The
342 combination of the knowledge of general curve shapes and the location of
343 performance related factors gives a further insight into inconsistencies in
344 respect to maximum vGRF reported in some discrete point analysis studies as
345 a performance related factor [4, 8, 30], while not in others [19, 21, 24]. In light
346 of the subgroup findings, maximum vGRF represents different neuromuscular
347 capacities across each cluster. For cluster 1 and 2 (shapes with low initial
348 vGRFs), maximum vGRF represents the ability to generate vGRFs at the
349 end of the movement cycle as the ankle, knee and hip joint extend towards
350 full extension; while it represents the ability to generate vGRFs quickly (1-15
351 %) after the start of the concentric phase for cluster 3 and 4. Consequently,
352 maximum vGRF cannot be compared using a single group analysis because
353 even if an analysis of peak vGRF accounts for different modalities of a vGRF
354 curve, it can fail to examine comparable neuromuscular capacities. The
355 present work indicates that classifying a sample of individuals into multiple
356 clusters can overcome limitations of a group analysis and hence enhances
357 the understanding of the underlying neuromuscular movement's strategies
358 during a movement task.

359 **5. Conclusion**

360 K-means clustering utilizing normalized subject scores appears to be the
361 most suitable technique for clustering vGRF curves, while hierarchical clus-
362 tering also showed a high level of suitability. Further, when clustering curve
363 shapes, it is extremely important to normalize subject scores, by transform-
364 ing them into their correlation matrix, before using a clustering technique.
365 The subgroup analysis should be used in preference to a single group anal-
366 ysis because it explained greater variances in the dependent variable (jump
367 height), indicating different movement strategies for which some different
368 performance determining factors were evident. These findings may explain,
369 at least in part, the contrasting findings between previous studies that ex-
370 amined vGRF during vertical jumping at the single group level of analysis.

371 **6. Conflict of interest statement**

372 The authors declare that no conflict of interest is associated with the
373 present study.

374 **7. Acknowledgements**

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